

## Eric M. Rains

### Work Address

Department of Mathematics  
California Institute of Technology  
1200 E. California Blvd.  
MC 253-37  
Pasadena, CA 91125  
Internet: rains@caltech.edu

### Home Address

500 E. Del Mar Blvd. #14  
Pasadena, CA 91101

### Education

Case Western Reserve University  
Graduated May 1991  
Bachelor of Arts with concentration in Physics, summa cum laude  
Bachelor of Science, summa cum laude  
Master of Science in Mathematics

Cambridge University  
Graduated June 1992  
Certificate of Advanced Study in Mathematics

Harvard University  
Graduated June 1995  
Doctor of Philosophy in Mathematics  
Thesis advisor: Persi Diaconis  
Thesis title: *Topics in Probability on Compact Lie Groups*

### Experience

July 2007–present: Professor of Mathematics, California Institute of Technology  
Fall 2011: Visiting Professor,  
Department of Mathematics  
Massachusetts Institute of Technology

July 2003–June 2007: Professor, Department of Mathematics,  
University of California at Davis

Fall 2006: Visiting Professor,  
Department of Mathematics and Statistics  
University of Melbourne

April 2002–August 2003: Mathematician,  
Center for Communications Research–Princeton

Fall 2002: Visiting Associate and Lecturer,  
Mathematics Department and Institute for Quantum Information,  
California Institute of Technology

April 2001–March 2002: Principal Member of Technical Staff,  
AT&T Laboratories–Research

September 1996–March 2001: Senior Member of Technical Staff,  
AT&T Laboratories–Research

June 1995–September 1996: Mathematician, CCR–Princeton

## Awards, Honors, and Funding

National Science Foundation Grant DMS-1500806  
“Noncommutative geometry and elliptic special functions”  
AMS Invited Address at the Joint Mathematics Meeting, 2012 (Boston)  
Invited talk at ICM 2010, combinatorics section  
Plenary talk at the Western Sectional AMS meeting, Fall 2007  
National Science Foundation Grant DMS-1001645  
“Elliptic special functions”  
National Science Foundation Grant DMS-0401387  
“Multivariate special functions”  
Three year grant starting July 2004, extended as DMS-0833464.  
The best paper of the year award 2005 in difference equations, awarded by  
the International Society of Difference Equations for [42, 41, 40]  
National Science Foundation Fellowship (Fall 1992-Spring 1995)  
Churchill Scholarship (for one year of study in Mathematics and Physics  
at Cambridge University, England, Fall 1991-Spring 1992)  
Inducted into Phi Beta Kappa (1991)  
8th place in William Lowell Putnam Examination (1990)

## Publications

- [1] C. M. Ormerod and E. M. Rains. Commutation relations and discrete Garnier systems. *SIGMA Symmetry Integrability Geom. Methods Appl.*, 12:Paper No. 110, 50, 2016.
- [2] P. Etingof and E. Rains. On Cohen-Macaulayness of algebras generated by generalized power sums. *Comm. Math. Phys.*, 347(1):163–182, 2016.
- [3] A. Okounkov and E. Rains. Noncommutative geometry and Painlevé equations. *Algebra Number Theory*, 9(6):1363–1400, 2015.
- [4] M. Bhargava, D. M. Kane, H. W. Lenstra, Jr., B. Poonen, and E. Rains. Modeling the distribution of ranks, Selmer groups, and Shafarevich-Tate groups of elliptic curves. *Camb. J. Math.*, 3(3):275–321, 2015.
- [5] F. J. van de Bult and E. M. Rains. Limits of elliptic hypergeometric biorthogonal functions. *J. Approx. Theory*, 193:128–163, 2015.
- [6] E. Rains and S. Ruijsenaars. Difference operators of Sklyanin and van Diejen type. *Comm. Math. Phys.*, 320(3):851–889, 2013.
- [7] E. M. Rains and M. J. Vazirani. Deformations of permutation representations of Coxeter groups. *J. Algebraic Combin.*, 37(3):455–502, 2013.
- [8] E. M. Rains. Elliptic Littlewood identities. *J. Combin. Theory Ser. A*, 119(7):1558–1609, 2012.

- [9] P. J. Forrester and E. M. Rains. A Fuchsian matrix differential equation for Selberg correlation integrals. *Comm. Math. Phys.*, 309(3):771–792, 2012.
- [10] B. Poonen and E. Rains. Random maximal isotropic subspaces and Selmer groups. *J. Amer. Math. Soc.*, 25(1):245–269, 2012.
- [11] B. Poonen and E. Rains. Self cup products and the theta characteristic torsor. *Math. Res. Lett.*, 18(6):1305–1318, 2011.
- [12] P. Etingof and E. Rains. On algebraically integrable differential operators on an elliptic curve. *SIGMA Symmetry Integrability Geom. Methods Appl.*, 7:Paper 062, 19, 2011.
- [13] E. M. Rains. An isomonodromy interpretation of the hypergeometric solution of the elliptic Painlevé equation (and generalizations). *SIGMA Symmetry Integrability Geom. Methods Appl.*, 7:Paper 088, 24, 2011.
- [14] E. M. Rains. The homology of real subspace arrangements. *J. Topol.*, 3(4):786–818, 2010.
- [15] A. Borodin, V. Gorin, and E. M. Rains.  $q$ -distributions on boxed plane partitions. *Selecta Math. (N.S.)*, 16(4):731–789, 2010.
- [16] P. Etingof, A. Henriques, J. Kamnitzer, and E. Rains. The cohomology ring of the real locus of the moduli space of stable curves of genus 0 with marked points. *Ann. of Math. (2)*, 171(2):731–777, 2010.
- [17] E. M. Rains. Transformations of elliptic hypergeometric integrals. *Ann. of Math. (2)*, 171(1):169–243, 2010.
- [18] A. Lascoux, E. M. Rains, and S. O. Warnaar. Nonsymmetric interpolation Macdonald polynomials and  $\mathfrak{gl}_n$  basic hypergeometric series. *Transform. Groups*, 14(3):613–647, 2009.
- [19] È. M. Raĩns and V. P. Spiridonov. Determinants of elliptic hypergeometric integrals. *Funktsional. Anal. i Prilozhen.*, 43(4):67–86, 2009.
- [20] E. M. Rains. The action of  $S_n$  on the cohomology of  $\overline{M}_{0,n}(\mathbb{R})$ . *Selecta Math. (N.S.)*, 15(1):171–188, 2009.
- [21] E. M. Rains. Limits of elliptic hypergeometric integrals. *Ramanujan J.*, 18(3):257–306, 2009.
- [22] A. Günther, G. Nebe, and E. M. Rains. Clifford-Weil groups of quotient representations. *Albanian J. Math.*, 2(3):159–169, 2008.
- [23] A. Henderson and E. Rains. The cohomology of real De Concini-Procesi models of Coxeter type. *Int. Math. Res. Not.*, (7):Art. ID rnn001, 29, 2008.
- [24] P. Etingof and E. Rains. New deformations of group algebras of Coxeter groups. II. *Geom. Funct. Anal.*, 17(6):1851–1871, 2008.

- [25] E. M. Rains and M. Vazirani. Vanishing integrals of Macdonald and Koornwinder polynomials. *Transform. Groups*, 12(4):725–759, 2007.
- [26] P. J. Forrester and E. M. Rains. Symmetrized models of last passage percolation and non-intersecting lattice paths. *J. Stat. Phys.*, 129(5-6):833–855, 2007.
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- [28] P. Etingof, A. Oblomkov, and E. Rains. Generalized double affine Hecke algebras of rank 1 and quantized del Pezzo surfaces. *Adv. Math.*, 212(2):749–796, 2007.
- [29] P. Etingof, F. Latour, and E. Rains. On central extensions of preprojective algebras. *J. Algebra*, 313(1):165–175, 2007.
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